

Stopping rules

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1 Stopping rules

On-line references:

[When Has Estimation Reached A Steady State \[2\] interactive](#)

[Stopping Rules in Estimation and Simulation \(interactive Guide chapter\)](#)

Processing examples follow.

1.1 Stopping Rules in Estimation

Aim:

Experiments with stopping rules in estimation.

Description:

Quasi-Bayes estimation is done with and without stopping rules and results are compared (prediction-error norm).

Specification:

System: realization of *ndat* two-dimensional data generated by normal *static mixture* with *ncom* components determined by *seed*.

The components have common diagonal covariance with the diagonal filled by *diac*. Their centers are uniformly positioned on unit circle. Component weights are linearly decreasing. [View details in code.](#)

Decision: when to stop experiments.

Experience: *ndat* two-dimensional data records (collected on two *channels*); correct system *structure*.

Ignorance: model parameters; future system outputs; quality of compared estimation algorithms.

Loss function: negative *v-log-likelihood* normalized by number of processed data; *prediction-errors norm*; contour plots of the posterior pdf on estimated parameters.

Recommended experiments:

Observe stop time for different values of *threshold*= 0.001, 0.01, 0.1

[Run example](#)[description](#)[view code](#)[Contents](#)

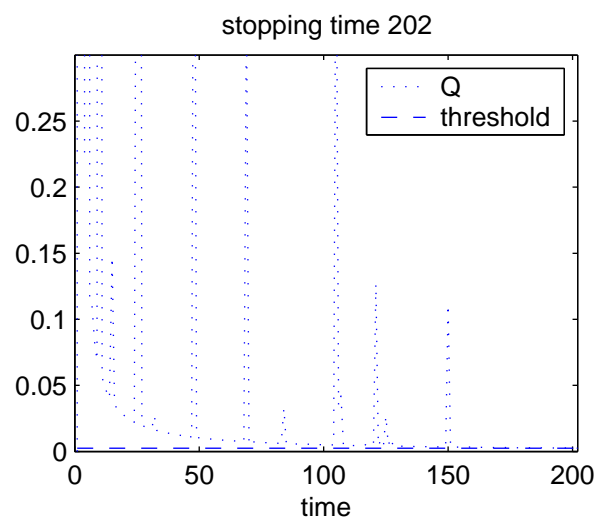
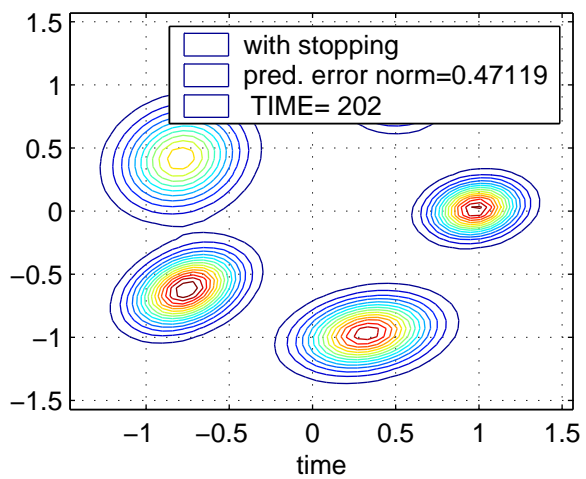
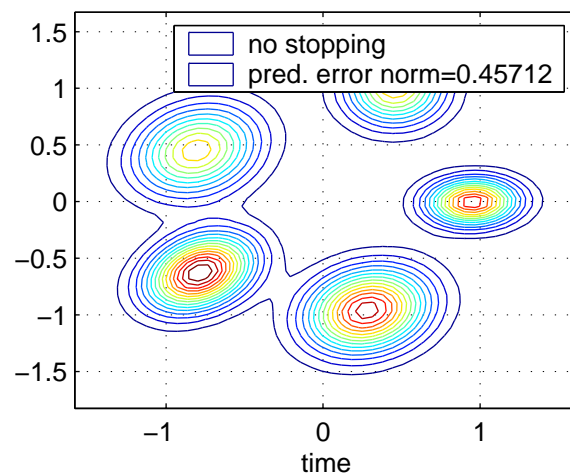
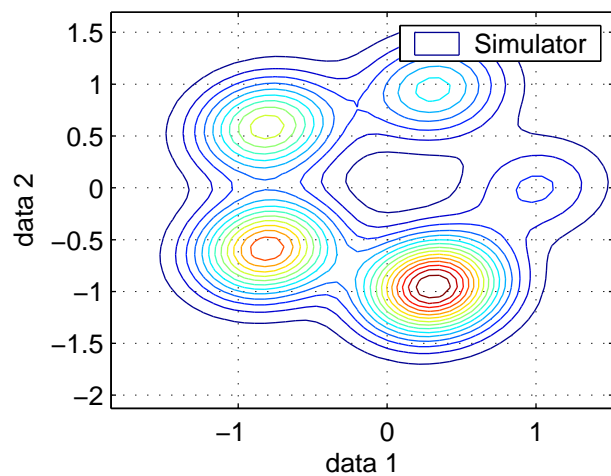


Figure 1: Results with defaults

1.2 Stopping Rules in Simulation

Aim:

Experiments with stopping rules in simulation.

Description:

Quasi-Bayes estimation is done with and without stopping rules and results are compared (prediction-error norm).

Specification:

System: realization of *ndat* two-dimensional data generated by normal *static mixture* with *ncom* components determined by *seed*.

The components have common diagonal covariance with the diagonal filled by *diac*. Their centers are uniformly positioned on unit circle. Component weights are linearly decreasing. [View details in code.](#)

Decision: when to stop experiments.

Experience: *ndat* two-dimensional data records (collected on two *channels*); correct system *structure*.

Ignorance: model parameters; future system outputs; quality of compared estimation algorithms.

Loss function: negative *v-log-likelihood* normalized by number of processed data; *prediction-errors norm*; contour plots of the posterior pdf on estimated parameters.

Recommended experiments:

Observe stop time for different values of *threshold*= 0.001, 0.01, 0.1

[Run example](#)[description](#)[help on simeval](#)[view code](#)[Contents](#)

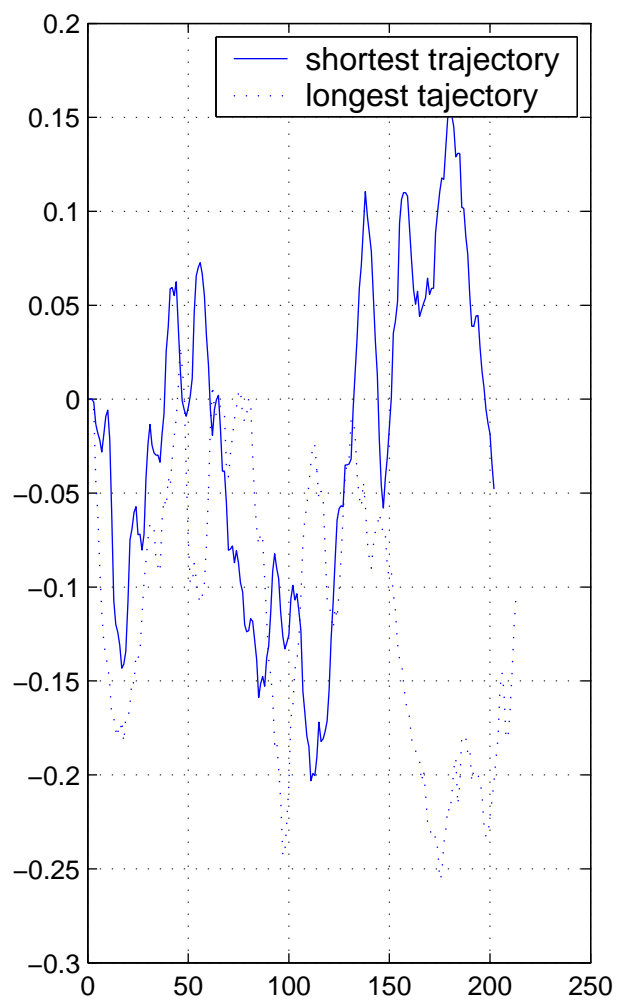
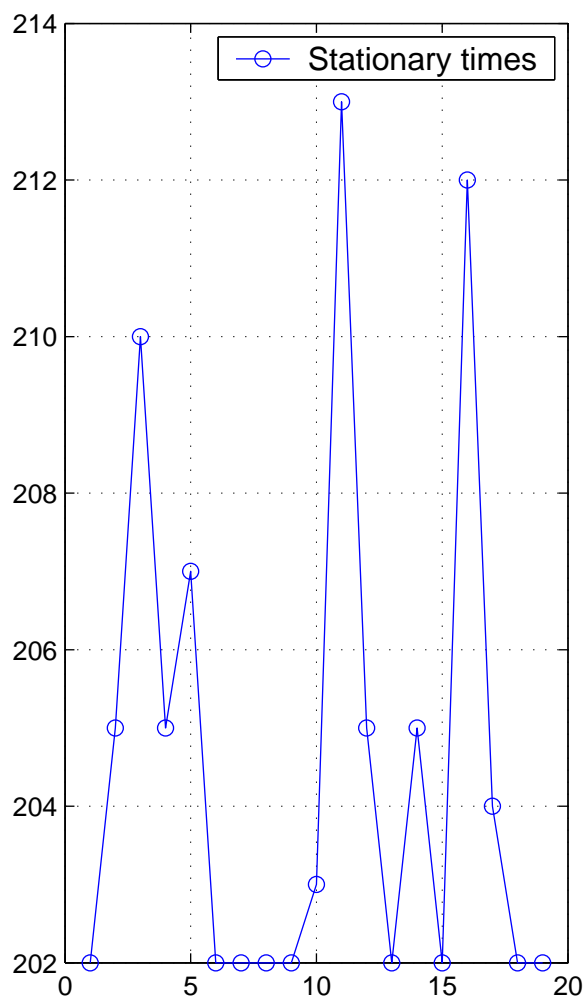


Figure 2: Results with defaults

1.3 Comparison of Mixture Estimation Algorithms

Aim:

To choose a learning algorithm and its tuning knobs adequate to the considered system. The algorithms compared are [projection method \(PB\)](#), [quasi-Bayes, see Section 6.5.1{158} \(QB\)](#), [batch quasi-Bayes, see section 6.5.12{165} \(BQB\)](#) and [forgetting branching, see Algorithm 6.4.31{141} \(BFRG\)](#), each of which approximately estimates mixture of a fixed known structure. [Two functions designed using stopping rules](#) are added: PX (projection method) and QX (quasi-Bayes with stopping rules).

Description:

Observed data are generated by a static simulated mixture. They are used for estimation of mixture models via the learning algorithms compared. Their performance is influenced by the number of iterations [niter](#) and forgetting rate [frg](#). The forgetting branching uses additionally an alternative small forgetting rate [frga](#).

Specification:

System: realization of [ndat](#) two-dimensional data generated by normal [static mixture](#) with [ncom](#) components determined by [seed](#).

The components have common diagonal covariance with the diagonal filled by [diac](#). Their centers are uniformly positioned on unit circle. Component weights are linearly decreasing. [View details in code](#).

Decision: one-step-ahead output predictions, generalized Bayesian estimation of mixture parameters.

Experience: [ndat](#) two-dimensional data records (collected on two [channels](#)); correct system [structure](#).

Ignorance: model parameters; future system outputs; quality of compared estimation algorithms.

Loss function: negative [v-log-likelihood](#) normalized by number of processed data; [prediction-errors norm](#); contour plots of the posterior pdf on estimated parameters.

Recommended experiments:

Performance of the inspected heuristic algorithms vary with extent of data, noise level, system complexity, behavior realization and optional knobs of algorithms. It is worth inspecting the influence of

- extent of learning data, say [ndat](#) = 500, 300, 200
- system-noise variance, [diac](#) = 0.5, 1
- estimated system complexity, [ncom](#) = 10, 20
- behavior realization, [seed](#) = any positive integer
- number of iterations, [niter](#) = 10, 30, 100 (computational time increases linearly)
- involved forgetting factors on quality of branching-by-forgetting, [frg](#) = 0.99, 0.999
[frga](#) = 0.5, 0.9

[Run example](#)[help on mixest](#)[view code](#)[Contents](#)

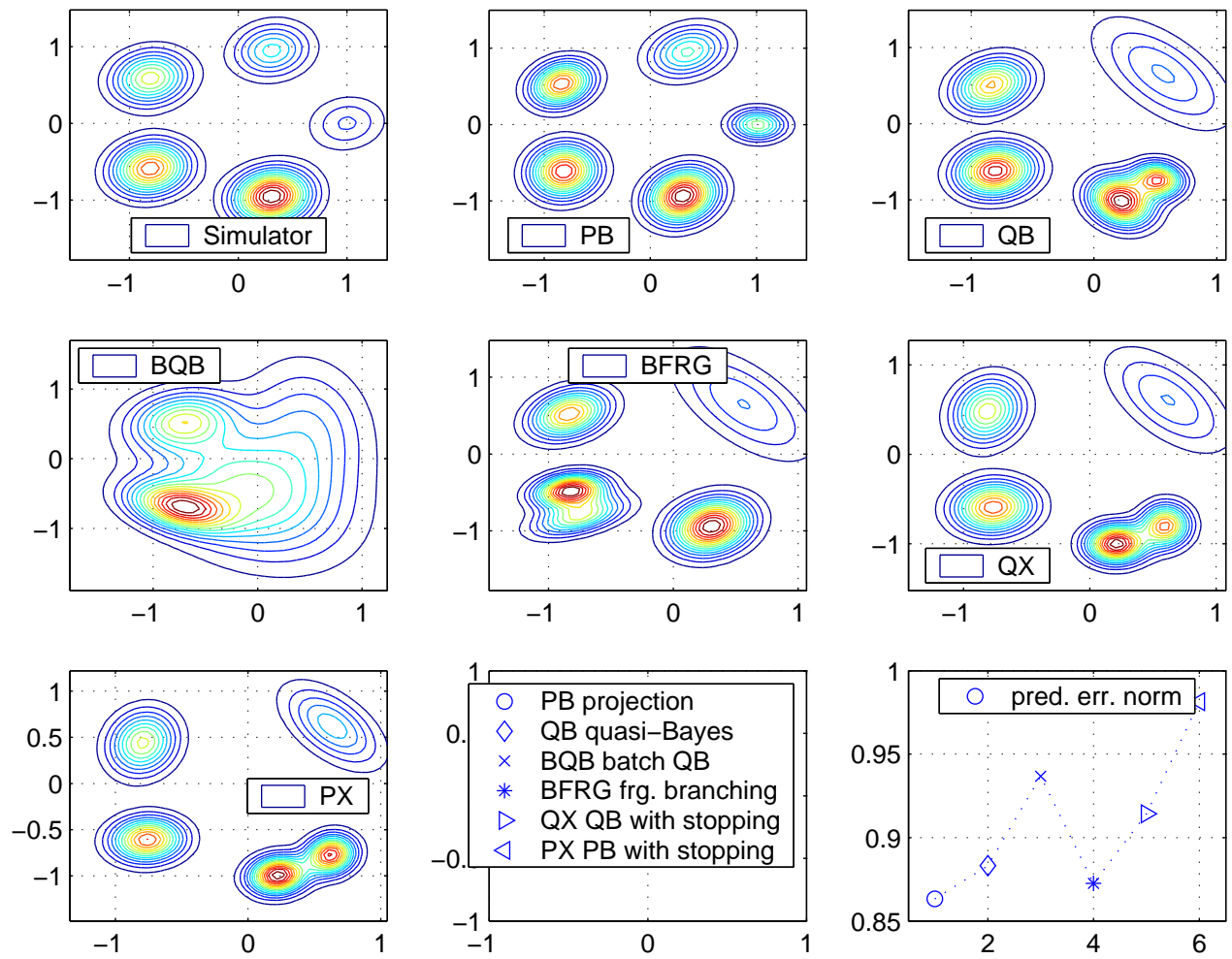


Figure 3: Results with defaults

1.4 Stopping Rules in Initialization

Aim:

Experiments with stopping rules in initialization.

Description:

An estimation method is selected specifying *opt*:

- 'p' iterative projection based estimation ([QB](#))
- 'q' iterative quasi-Bayes mixture estimation ([QB](#))
- 'b' iterative batch quasi-Bayes mixture estimation ([BQB](#))
- 'f' iterative mixture estimation based on forgetting branching ([BFRG](#))
- 'P' iterative projection with stopping rules ([PX](#))
- 'Q' iterative projection with stopping rules ([QX](#))
- 'n' without iterative estimation (default) (single path of [QB](#))

Then *mixinit* is called and individual iterations are displayed. As a measure of quality, [prediction-error norm](#) is displayed.

Specification:

System: realization of [ndat](#) two-dimensional data generated by normal [static mixture](#) with [ncom](#) components determined by [seed](#).

The components have common diagonal covariance with the diagonal filled by [diac](#). Their centers are uniformly positioned on unit circle. Component weights are linearly decreasing. [View details in code](#).

Decision: when to stop estimation internally called by *mixinit*.

Experience: [ndat](#) two-dimensional data records.

Ignorance: model structure.

Loss function: negative *v*-log-likelihood

Recommended experiments:

Observe stop time for different values of *threshold*= 0.001, 0.01, 0.1

[Run example](#)[description](#)[view code](#)[Contents](#)

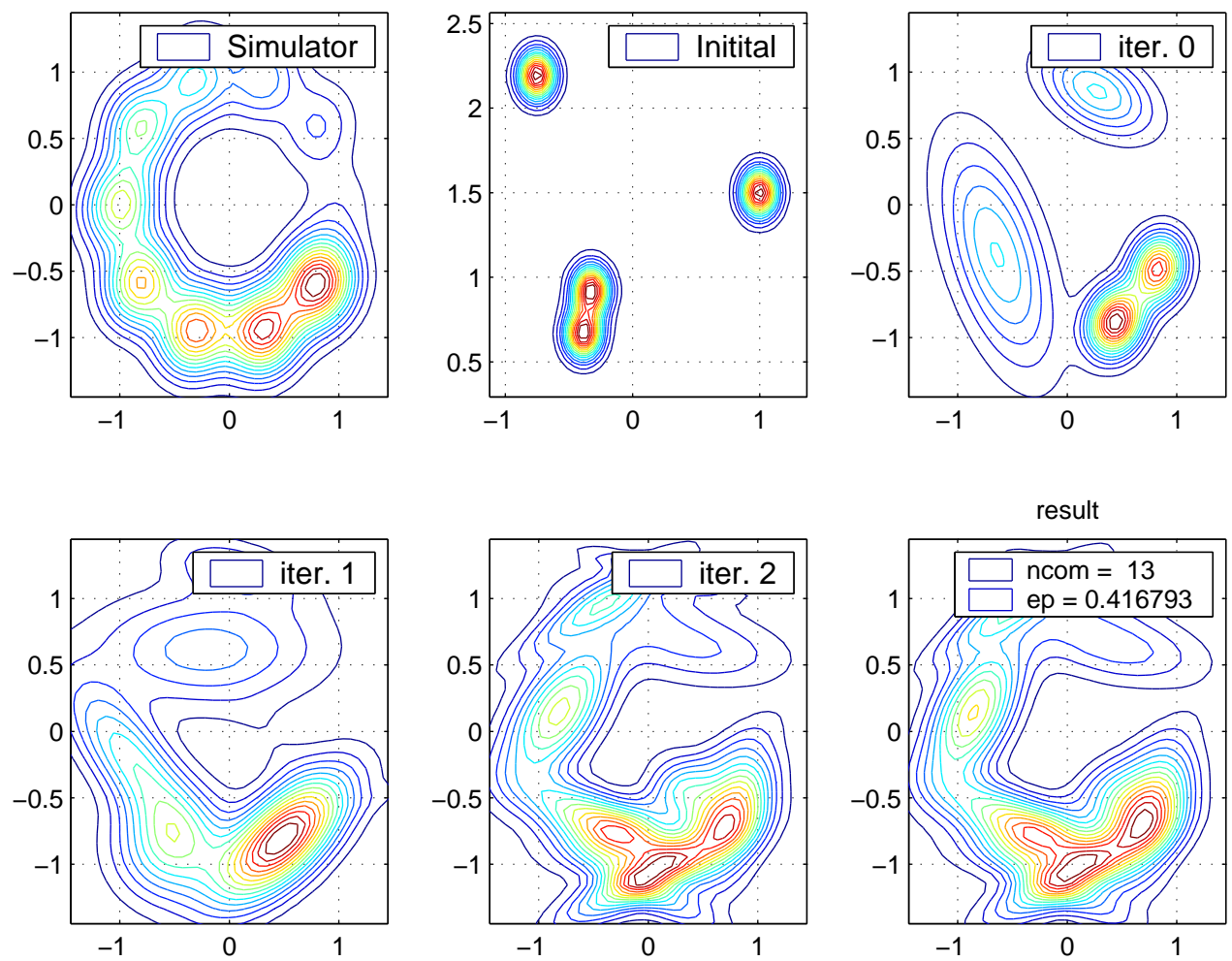


Figure 4: Results with defaults

References

- [1] M. Kárný, J. Böhm, T.V. Guy, L. Jirsa, I. Nagy, P. Nedoma, and L. Tesař, *Optimized Bayesian Dynamic Advising: Theory and Algorithms*, Springer, London, 2004, to appear.
- [2] M. Kárný, J. Kracík, I. Nagy, and P. Nedoma, “When Has Estimation Reached A Steady State? The Bayesian Sequential Test”, *International Journal of Adaptive Control and Signal Processing*, 2004, accepted.